gristmill Documentation

Release 0.3.0

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ONE

INTRODUCTION

The gristmill package is a pure Python package based on drudge for automatic code generation and optimization, with emphasis on tensor contraction operations.

TWO

RELEASE HISTORY

2.1 0.2.0

This is mostly a bug fix release. Problems in the handling of bounds in Fortran printer and in the treatment purely scalar intermediates without any external indices are fixed. And the handling of summations are improved with less intermediates by removing duplicated and shallowly-defined ones. Most importantly, the automatic result checker has been fixed.

2.2 0.3.0

This release primarily features the addition of product optimization strategies. It was hoped that the new default SEARCHED will provide big improvement over the previous behaviour, which can now be accessed by BEST. Unfortunately, the improvement is only marginal. But the new strategy GREEDY could be used for large problems defying deeper optimizations.

THREE

API REFERENCE

The gristmill package can be divided into two orthogonal parts,

The evaluation optimization part, which transforms tensor definitions into a mathematically equivalent definition sequence with less floating-point operations required.

The code generation part, which takes tensor definitions, either optimized or not, into computer code snippets.

3.1 Evaluation Optimization

```
gristmill.optimize (computs: typing.Iterable[drudge.drudge.TensorDef], substs=None, interm_fmt='tau^{}', simplify=True, strategy=<Strategy.SEARCHED: 2>) \rightarrow typing.List[drudge.drudge.TensorDef]
Optimize the valuation of the given tensor contractions.
```

This function will transform the given computations, given as tensor definitions, into another list computations mathematically equivalent to the given computation while requiring less floating-point operations (FLOPs).

Parameters

- **computs** The computations, can be given as an iterable of tensor definitions.
- **substs** A dictionary for making substitutions inside the sizes of ranges. All the ranges need to have size in at most one undetermined variable after the substitution so that they can be totally ordered.
- interm fmt The format for the names of the intermediates.
- **simplify** If the input is going to be simplified before processing. It can be disabled when the input is already simplified.
- **strategy** The optimization strategy, as explained in *Strategy*.

class gristmill.Strategy

The optimization strategy for tensor contractions.

This enumeration type gives possible options for the optimization strategy for tensor contractions. Supported values includes,

GREEDY The contraction will be optimized greedily. This should only be used for large inputs where the other strategies cannot finish within a reasonable time.

BEST The global minimum of each tensor contraction will be found by the advanced algorithm in gristmill. And only the optimal contraction(s) will be kept for the summation optimization.

SEARCHED The same strategy as BEST will be attempted for the optimization of contractions. But all evaluations searched in the optimization process will be kept and considered in subsequent summation optimizations.

ALL All possible contraction sequences will be considered for all contractions. This can be extremely slow. But it might be helpful for manageable problems.

```
gristmill.verify_eval_seq (eval_seq: typing.Sequence[drudge.drudge.drudge.TensorDef], res: typing.Sequence[drudge.drudge.TensorDef], simplify=False) \rightarrow bool Verify the correctness of an evaluation sequence for the results.
```

The last entries of the evaluation sequence should be in one-to-one correspondence with the original form in the res argument. This function returns True when the evaluation sequence is symbolically equivalent to the given raw form. When a difference is found, ValueError will be raised with relevant information.

Note that this function can be very slow for large evaluations. But it is advised to be used for all optimizations in mission-critical tasks.

Parameters

- **eval_seq** The evaluation sequence to verify, can be the output from <code>optimize()</code> directly.
- res The original result to test the evaluation sequence against. It can be the input to optimize() directly.
- simplify If simplification is going to be performed after each step of the backsubstitution. It is advised for larger complex evaluations.

This function gives the count of floating-point operations, addition and multiplication, involved by the evaluation sequence. Note that the cost of copying and initialization are not counted. And this function is only applicable where the amplitude of the terms are simple products.

Parameters

- eval_seq The evaluation sequence whose FLOP cost is to be estimated. It should be given as an iterable of tensor definitions.
- **leading** If only the cost terms with leading scaling be given. When multiple symbols are present in the range sizes, terms with the highest total scaling is going to be picked.
- ignore_consts If the cost of scaling with constants can be ignored. $2x_iy_j$ could count as just one FLOP when it is set, otherwise it would be two.

3.2 Code generation

```
class gristmill.BasePrinter(scal_printer:
                                                              sympy.printing.printer.Printer,
                                      dexed proc cb=<function
                                                                             BasePrinter.<lambda>>,
                                      add globals=None,
                                                              add filters=None,
                                                                                     add tests=None,
                                      add_templ=None)
     The base class for tensor printers.
                                        sympy.printing.printer.Printer,
                                                                           indexed_proc_cb=<function
        _init___(scal_printer:
                 BasePrinter.<lambda>>,
                                            add_globals=None,
                                                                 add_filters=None,
                                                                                     add tests=None,
```

Initializes a base printer. Parameters

add_templ=None)

• scal_printer – The SymPy printer for scalar quantities.

• indexed_proc_cb - It is going to be called with context nodes with base and indices (in both the root and for each indexed factors, as described in transl()) to do additional processing.

 $transl(tensor_def: drudge.drudge.TensorDef) \rightarrow types.SimpleNamespace$

Translate tensor definition into context for template rendering.

This function will translate the given tensor definition into a simple namespace that could be easily used as the context in the actual Jinja template rendering.

The context contains fields,

base A printed form for the base of the tensor definition.

indices A list of external indices. For each entry, keys index and range are present to give the printed form of the index and the range it is over. For convenience, lower, upper, and size have the printed form of lower/upper bounds and the size of the range. We also have lower_expr, upper_expr, and size_expr for the unprinted expression of them.

terms A list of terms for the tensor, with each entry being a simple namespace with keys,

sums A list of summations in the tensor term. Its entries are in the same format as the external indices for tarrays.

phase + sign or - sign. For the phase of the term.

numerator The printed form of the numerator of the coefficient of the term. It can be a simple 1 string.

denominator The printed form of the denominator.

indexed_factors The indexed factors of the term. Each is given as a simple namespace with key
base for the printed form of the base, and a key indices giving the indices to the key, in the
same format as the indices field of the base context.

other_factors Factors which are not simple indexed quantity, given as a list of the printed form directly.

The actual content of the context can also be customized by overriding the proc_ctx() in subclasses.

Make additional processing of the rendering context.

This method can be override to make additional processing on the rendering context described in trans1() to perform additional customization or to make more information available.

It will be called for each of the terms during the processing. And finally it will be called again with the term given as None for a final processing.

By default, the indexed quantities nodes are processed by the user-given call-back.

render (templ_name: str, ctx: types.SimpleNamespace) → str

Render the given context for the given template.

Meaningful subclass methods can call this function for actual functionality.

weakref

list of weak references to the object (if defined)

```
sympy.printing.printer.Printer,
class gristmill.ImperativeCodePrinter(scal_printer:
                                                                              global_indent=1,
                                                     print indexed cb,
                                                      dent size=4,
                                                                       max \ width=80,
                                                                                            line cont=",
                                                                                             stmt_end=".
                                                      breakable\_regex='(\s^*[+-]\s^*)',
                                                      add globals=None,
                                                                                        add filters=None,
                                                      add tests=None, add templ=None, **kwargs)
     Printer for automatic generation of naive imperative code.
     This printer supports the printing of the evaluation of tensor expressions by simple loops and arithmetic opera-
     tions.
     This is mostly a base class that is going to be subclassed for different languages. For each language, mostly just
     the options for the language could be given in the super initializer. Most important ones are the printer for the
     scalar expressions and the formatter of loops, as well as some definition of literals and operators.
                                  sympy.printing.printer.Printer, print_indexed_cb, global_indent=1, in-
      __init__(scal_printer:
                  dent_size=4, max_width=80, line_cont=", breakable_regex='(\\s*/+-\\\s*)', stmt_end=",
                  add_globals=None, add_filters=None, add_tests=None, add_templ=None, **kwargs)
           Initialize the automatic code printer.
           scal_printer A sympy printer used for the printing of scalar expressions.
           print_indexed_cb It will be called with the printed base, and the list of indices (as described in
               BasePrinter.transl()) to return the string for the printed form. This will be called after the
               given processing of indexed nodes.
           global_indent The base global indentation of the generated code.
           indent size The size of the indentation.
           max width The maximum width for each line.
           line cont The string used for indicating line continuation.
           breakable_regex The regular expression used to break long expressions.
           stmt_end The ending of the statements.
           index_paren The pair of parenthesis for indexing arrays.
           All options to the base class BasePrinter are also supported.
     proc_ctx (tensor_def: drudge.drudge.TensorDef, term: typing.Union[drudge.term.Term, NoneType],
                  tensor_entry: types.SimpleNamespace, term_entry: typing.Union[types.SimpleNamespace,
                  NoneType])
           Process the context.
           The indexed nodes will be printed by user-given printer and given to indexed attributes of the same node.
           Also the term contexts will be given an attribute named amp for the whole amplitude part put together.
     print eval (ctx: types.SimpleNamespace)
           Print the evaluation of a tensor definition.
gristmill.CCodePrinter
     alias of wrapper
class gristmill.FortranPrinter(openmp=True, **kwargs)
```

In this class, just some parameters for the *new* Fortran programming language is fixed relative to the base

Fortran code printer.

ImperativeCodePrinter.

_init__ (openmp=True, **kwargs)
Initialize a Fortran code printer.

The printer class, the name of the template, and the line continuation symbol will be set automatically.

Parameters

- tensor_defs The tensor definitions to print.
- **decl_type** The type to be declared for the tarrays.
- explicit_bounds If the lower and upper bounds should be written explicitly in the declaration.

Returns

- decls The list of declaration strings.
- evals The list of evaluation strings.

```
print_decl (ctx, decl_type, explicit_bounds)
```

Print the Fortran declaration of the LHS of a tensor definition.

A string will be returned that forms the naive declaration of the given tarrays as local variables.

```
class gristmill.EinsumPrinter(**kwargs)
```

Printer for the einsum function.

For tensors that are classical tensor contractions, this printer generates code based on the NumPy einsum function. For contractions supported, the code from this printer can also be used for Tensorflow.

```
___init___(**kwargs)
Initialize the printer.
```

All keyword arguments are forwarded to the base class BasePrinter.

 $print_eval$ (tensor_defs: typing.Iterable[drudge.drudge.TensorDef], base_indent=4) \rightarrow str Print the evaluation of the tensor definitions.

Parameters

- tensor_defs The tensor definitions for the evaluations.
- base_indent The base indent of the generated code.

Returns

Return type The code for evaluations.

FOUR

INDICES AND TABLES

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